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Activity on Momentum Transport

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Small scale localization in the Large Eddy Simulation of a compressible turbulent jet at

$$M = 5$$

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Motivation: LES for high Re turbulent flows

- Compressible turbulent flows may have very high Reynolds numbers e.g.: astrophysical jets have $Re > 10^{10} \div 10^{13}$ and M up to $50 \div 100$
- ullet hopefully, the large scales only may be simulated ⇒ explicit LES modeling is needed
- ullet regions where turbulence is fully developed do not fill the entire domain ⇒ a tool to detect such regions is needed to insert LES models
- LES and shock capturing are not compatible (Ducros, 1999) \Rightarrow explicit numerical dissipation
- is opportune to suppress LES subgrid terms \Rightarrow detection sensors are necessary to locate the shock regions, where it

Detection of turbulent regions with small (under-resolved) scale

The only model that attempts to locate regions under-resolved turbulent regions is the Selective Structure Function model by Lesieur et al. (1996-1999). It is based on:

$$f(\langle \boldsymbol{\omega} \rangle) = \frac{\langle \boldsymbol{\omega} \rangle \cdot \langle \langle \boldsymbol{\omega} \rangle \rangle_{2\delta}}{|\langle \boldsymbol{\omega} \rangle| |\langle \langle \boldsymbol{\omega} \rangle \rangle_{2\delta}|} \in [-1, 1]$$

when f is far to $1 \Rightarrow$ subgrid terms are inserted into filtered equations when f is close to $1 \Rightarrow$ no subgrid terms

Problems:

- ullet only the disalignement of vorticity vector on scale δ is used
- resolution it is not easy to define a threshold, which in turn seems to depend on the

Small scale localization criterium

in the simulation: When the flow is turbulent and not fully resolved, the smallest resolved scales

- are highly three-dimensional
- they are within the inertial range, and then:
- have significant level of energy
- ♦ non linear terms are important

So we consider the following functional

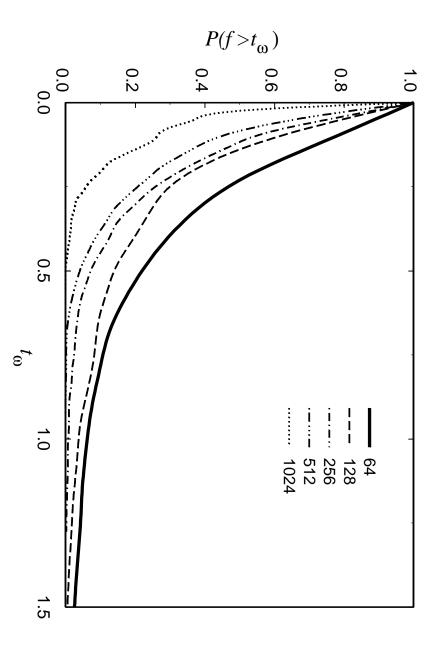
$$f(\langle \mathbf{u} \rangle, \langle \boldsymbol{\omega} \rangle) = \frac{|\langle \boldsymbol{\omega} \rangle \cdot \nabla \langle \mathbf{u} \rangle|}{|\langle \boldsymbol{\omega} \rangle|^2 + \varepsilon_0} \ge 0$$

Main features:

- \bullet information from only one filtering level with filter scale Δ is used.
- it is always positive, ranging from 0 when there is no flow to high values when there is high stretching in relation to enstrophy
- small constant $\varepsilon_0 > 0$ is used only to assure that $f \to 0$ when $\omega \to 0$.

A priori test: homogeneous isotropic turbulence

that f is larger than a given threshold t_{ω} is shown. from a DNS at $Re_{\lambda} = 280$, filtered at different resolutions: the probability The distribution of functional f has been tested on a turbulent field coming

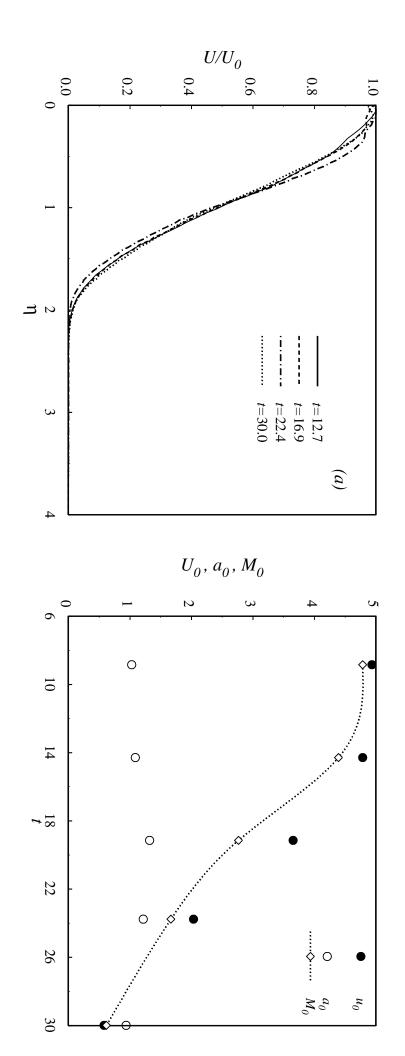


- Larger values of f have higher probability in less resolved fields.
- It is possible to define a threshold t_{ω} such that turbulence can be considered fully resolved when $f < t_{\omega}$ and unresolved when when $f > t_{\omega}$
- $t_{\omega} \approx 0.3$

Application to compressible jets simulations

temporal evolution of a 3D cylindrical jet: Functional f has been applied to results from numerical simulations of the

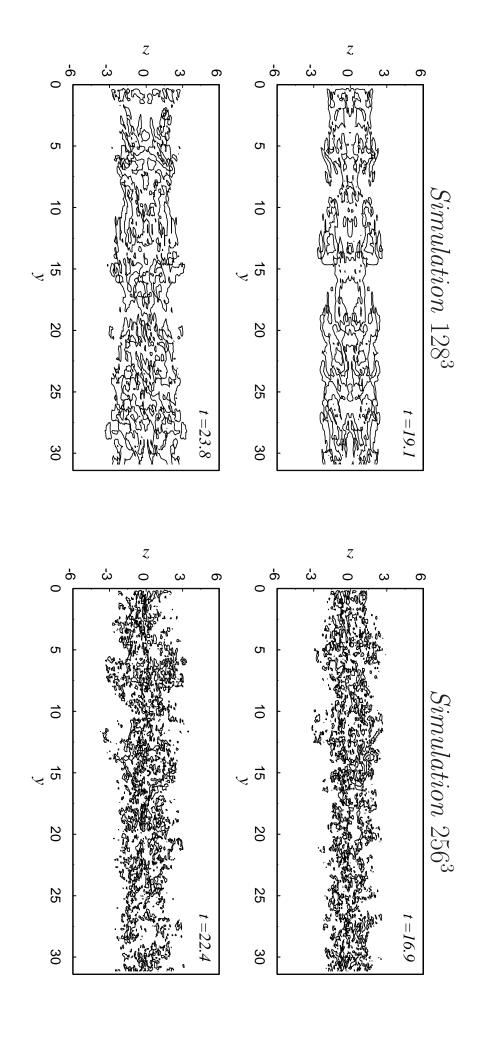
- Euler equations with PPM finite-volume numerical method, two resolutions: 128³ and 256^{3}
- Initial conditions: uniform jet with unstable perturbations
- Initial density ratio 0.1, initial jet Mach number M=5.



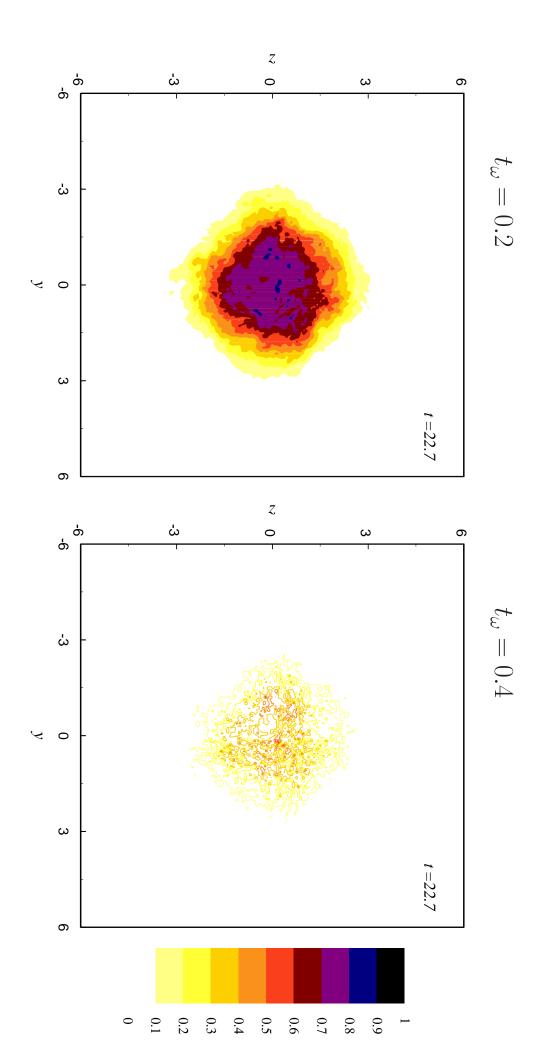
Distribution of functional f:

Areas where small, under-resolved, scales are present according to the cri-

$$f(\langle \mathbf{u} \rangle, \langle \boldsymbol{\omega} \rangle) > t_{\omega}, \quad t_{\omega} = 0.4$$



threshold t_{ω} on the functional f (simulation 256³, t=22.7): Fraction of space where sub-filter scales are present according to a selected

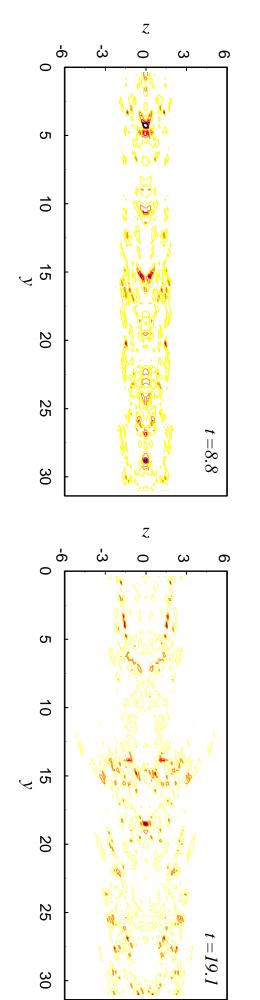


Shock detection

pation should be explicit. LES and numerical dissipation are not compatible, so that numerical dissi-

explicit numerical dissipation for shock capturing has been used: Following shock sensor proposed by Ducros et al. (1999) for the insertion of

$$s_j = \alpha \beta_j, \quad \alpha = \frac{(\nabla \cdot \langle \mathbf{u} \rangle)^2}{(\nabla \cdot \langle \mathbf{u} \rangle)^2 + \langle \omega \rangle^2}, \quad \beta_j = 4 \left| \frac{\langle p \rangle_{j+1} - 2 \langle p \rangle_j + \langle p \rangle_{j-1}}{\langle p \rangle_{j+1} + 2 \langle p \rangle_j + \langle p \rangle_{j-1}} \right|$$



- Strong compressions are present when the functional s is of order 1
- the subgrid scale model. coincide with setting of the numerical artifcial dissipation and setting aside The identification of the regions where the shocks are present will then

equations with terms of the kind This can be accomplished by structuring the Euler pseudo-direct-simulation

$$sD_a + (1-s)H(f-t_{\omega})\nabla \cdot \tau^{sgs}.$$

where H is the Heaviside step function.

Subgrid terms correction to jet pseudo-DNS simulations

spreading rate. We extimate the effect of the selective insertion of SGS terms on the jet

The ensemble average equation (Favre averages) for a temporal jet in the xdirection is

$$\frac{\partial \overline{\langle v_x \rangle_F}}{\partial t} = -\frac{\partial \overline{\langle v_x \rangle_F \langle v_r \rangle_F}}{\partial r} - \frac{\overline{\langle v_x \rangle_F \langle v_r \rangle_F}}{r} + \frac{\partial \overline{\tau_{xr}^{sgs}}}{\partial r} + \frac{\overline{\tau_{xr}^{sgs}}}{r}$$

A self-similar stage of evolution is reached after 10 time scales, so that:

$$\overline{\langle v_x \rangle_F} = U_0(t) f(\eta), \quad -\overline{\langle v_x \rangle_F \langle v_r \rangle_F} = \overline{\tau} = \tau_0(t) g(\eta), \quad \overline{\tau^{sgs}} = \overline{\tau_0^{sgs}}(t) g^{sgs}(\eta)$$
 where η is the similarity variable $\eta = r/\delta(t)$.

averaged balance, we obtain By inserting these similarity transformations in the longitudinal ensemble

$$f(\eta) - \frac{\delta' U_0}{\delta U_0'} \, \eta f'(\eta) = \frac{\overline{\tau_0(t)}}{\delta U_0'} \left[g'(\eta) + \frac{g(\eta)}{\eta} \right] + \frac{\overline{\tau_0^{sgs}(t)}}{\delta U_0'} \left[g^{sgs'}(\eta) + \frac{g^{sgs}(\eta)}{\eta} \right]$$

so that the temporal spreading rate is proportional to total stress, sum of the resolved Reynolds stress and of the sub-grid contribution:

$$\frac{d\delta}{dt} \propto \frac{\tau_0 + \tau_0^{5/3}}{U_0}$$

tion od SGS terms: Consequently we can relate the spreading rate with and without the correc-

$$\frac{d\delta}{dt} = \left(\frac{d\delta}{dt}\right)_{nc} \frac{\tau_0 + \tau_0^{sgs}}{\tau_0}$$

where the index nc (non corrected) indicates the spreading obtained from the under-resolved direct numerical simulation

Comparison with experimental results

spatial spreading rate: With a Taylor hypothesis the temporal spreading rate is transformed into a

 $\frac{d\delta}{dx} = \frac{d\delta}{dt}\frac{dt}{dx} = \frac{1}{U_0}\frac{d\delta}{dt}$

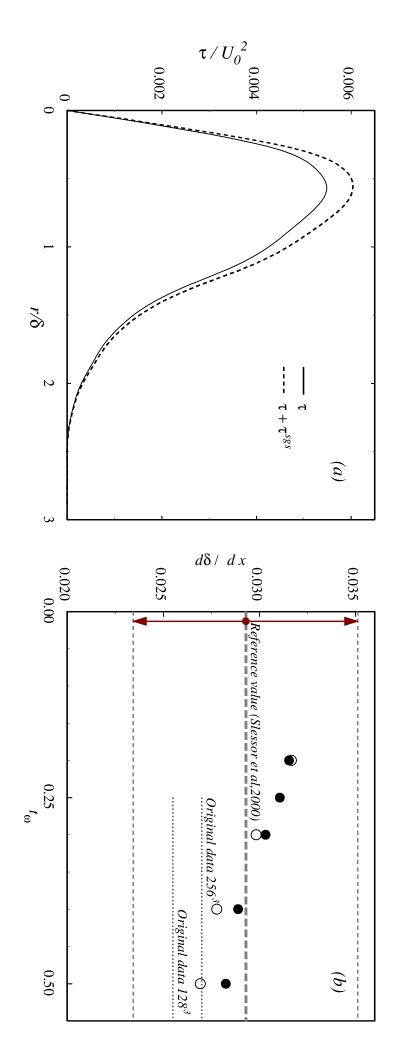
shear-layer growth by Slessor et al. (2001) in terms of parameter: Experimental comparison has been deduced from the scaling for compressible

$$\Pi_{c} = \max_{(i=1,2)} \left[\frac{1-\gamma_{i}}{a_{i}} \right] \Delta U$$

where

- $-\Delta U$ is the difference of the mean velocity in the jet and out of the jet,
- index i = 1, 2 represents the gases inside and outside the jet,
- $-\gamma_i$ are the isoentropic coefficients
- $-a_i$ are sound velocities

and then corrected with the density ratio (Brown & Roshko, 1974)



Final remarks

- A criterium for the localization of under-resolved regions in simulations of homogeneous turbulence. turbulent flows is proposed and is consistent with data from incompressible
- It is local
- It can be coupled with shock capturing numerical schemes with explicit artificial dissipation
- A priori tests on a global parameter (the jet growth rate) show that the selective introduction of subgrid terms brings to a spreading rate nearer to the experimental reference value